

Short communication

# Ti<sup>4+</sup> addition effect on $\alpha$ -Al<sub>2</sub>O<sub>3</sub> flakes synthesis using a mixture of boehmite and potassium sulfate

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## Abstract

Single-crystal  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> hexagonal flakes with a diameter of about 200 nm and 20 nm in thickness were obtained by mixing different molar ratios of potassium sulfate to boehmite and heating at 1000 °C. Co-doping 1 mol% TiO<sub>2</sub> can increase the shape anisotropy of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> hexagonal flakes, increasing the diameter to 400 nm. The effects of potassium sulfate, Fe<sub>2</sub>O<sub>3</sub> and TiO<sub>2</sub> on the phase transformation and morphology development of alumina were investigated using X-ray diffraction analysis (XRD), differential thermal analysis (DTA) and transmission electron microscopy (TEM). The results indicate that co-doping potassium sulfate, Fe<sup>3+</sup> and Ti<sup>4+</sup> can promote  $\gamma \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> phase transformation and change the morphology from a vermicular structure into hexagonal platelets. The shape anisotropy of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> hexagonal flakes can be increased by adding TiO<sub>2</sub> due to the segregation of Ti<sup>4+</sup> ions onto the surfaces of basal planes of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> single crystal particle.

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## 1. Introduction

$\alpha$ -Al<sub>2</sub>O<sub>3</sub> platelet powder has been widely applied in the industry, such as in metal or ceramic composite reinforcements [1,2], fillers in plastics for thermal conductivity enhancement [3], and pearlescent pigments [4], etc. Many methods have been used to prepare  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> platelet powder, including heating a mixture of Al<sub>2</sub>O<sub>3</sub> and aluminum fluoride [5], growth in an HF- $\gamma$ -Al<sub>2</sub>O<sub>3</sub> system [6], synthesis in a molten Na<sub>2</sub>SO<sub>4</sub> flux [7,8], K<sub>2</sub>SO<sub>4</sub> flux [9], synthesis in a 1,4-butanediol solution by seeding [10], synthesis using electrostatic spray-assisted chemical vapor deposition [11], and synthesis using the flux method in a microwave field [12].

In our previous study, we observed that single-crystal  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> hexagonal platelets can be prepared by heating a mixture of boehmite and potassium sulfate at below the salt melting temperature [13]. However, the shape anisotropy (diameter: 200 nm and thickness: 25 nm) is too low to significantly improve the mechanical and optical properties of composites.

In this study, the effects of the additives on the phase transformation and morphology development of alumina were investigated. The formation mechanism of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> hexagonal flakes was also examined.

## 2. Experimental

The feed stock materials were all technical grade Fe(NO<sub>3</sub>)<sub>3</sub>·9H<sub>2</sub>O, boehmite, TiCl<sub>4</sub> and K<sub>2</sub>SO<sub>4</sub>. 94 mol% boehmite, 5 mol% Fe(NO<sub>3</sub>)<sub>3</sub>·9H<sub>2</sub>O, and 1 mol% TiCl<sub>4</sub> aqueous solution were mixed and then dried at 120 °C. The dried gel powder was sieved through # 200 mesh, and was denoted as 1T. Sample 1T was mixed with different molar ratios of a potassium sulfate solution, followed by drying at 120 °C and calcined at 1000 °C (the heating rate was 4 °C/min, maintained for 2 h, and cooled in an oven furnace). The samples compositions and notations used in this study are shown in Table 1. After calcination, the samples were washed with distilled water thoroughly to remove the potassium sulfate. The washed powder was dried at 120 °C and then subjected to analysis. The thermal properties of the samples were measured by DTA (Netzsch STA 409C). The crystalline phase evolution was characterized by an X-ray diffraction analysis with a CuK $\alpha$  radiation (Siemens, D5000). The size and morphology of the

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Table 1  
Sample compositions and notations used in this study.

Samples	No.
95%Boehmite + 5% Fe <sup>3+</sup>	0T
94%Boehmite + 5% Fe <sup>3+</sup> + 1% Ti <sup>4+</sup>	1T
(95%Boehmite + 5% Fe <sup>3+</sup> )/XK <sub>2</sub> SO <sub>4</sub>	0TXK (X = 1–4)
(94%Boehmite + 5% Fe <sup>3+</sup> + 1%Ti <sup>4+</sup> )/XK <sub>2</sub> SO <sub>4</sub>	1TXK (X = 1–4)

powders were determined using TEM (JEOL JEM-3010, Tokyo, Japan). Semi-quantitative determination of the element content was detected by EDS (Noran, Voyager 1000), attached to the TEM.

### 3. Results and discussion

#### 3.1. Effects of additives on the thermal behavior and phase transformation of boehmite

Fig. 1 shows the DTA curves for boehmite added with various Fe<sup>3+</sup>, Ti<sup>4+</sup>, and K<sub>2</sub>SO<sub>4</sub> molar ratios. The endothermic peak at 500 °C and the exothermic peak at 1230 °C for pure boehmite are due to dehydration and  $\theta \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> phase transformation, respectively (Fig. 1(b)). For boehmite added with 5 mol% Fe<sup>3+</sup>, sample 0T, the phase transformation temperature of  $\theta \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> decreased to 1041 °C, falling by about 189 °C compared with pure boehmite. It was reported [14] that at 500–600 °C, Fe<sup>3+</sup> ions added in the boehmite were crystallized into hematite, which can act as a seed to decrease the activation energy of the  $\theta \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> phase transformation, hence decreasing the phase transformation temperature. The Fe effects on formation of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> from  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> were observed to result in Fe<sup>3+</sup> ions incorporation in the lattice structure of  $\gamma$ -Al<sub>2</sub>O<sub>3</sub>, and then formation of the Fe-rich clusters within the  $\gamma$ -Al<sub>2</sub>O<sub>3</sub> matrix, which increased the phase transformation rate to  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> [15]. The enhanced formation mechanism of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> by doping with Fe<sup>3+</sup> in this study agrees with the above findings. The hematite phase was not detected by XRD and no exothermic peak due to hematite crystallization (at 400–800 °C) was observed. It was found [16] that  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> phase transformation was dominated by Al<sup>3+</sup>

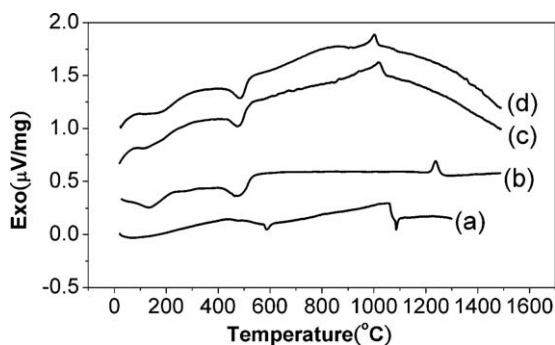


Fig. 1. DTA curves for boehmite added with various Fe<sup>3+</sup>, Ti<sup>4+</sup>, and K<sub>2</sub>SO<sub>4</sub> molar ratios (a) 1T4K, (b) boehmite, (c) 0T and (d) 1T.

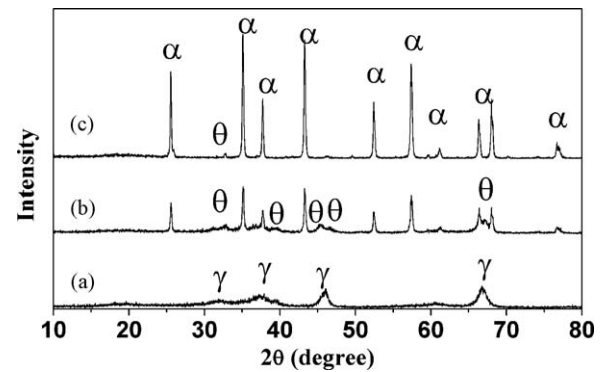


Fig. 2. XRD patterns for sample 1T calcined at various temperatures (a) 800 °C, (b) 900 °C and (C) 1000 °C ( $\alpha$ , $\alpha$ -Al<sub>2</sub>O<sub>3</sub>,  $\theta$ , $\theta$ -Al<sub>2</sub>O<sub>3</sub>,  $\gamma$ , $\gamma$ -Al<sub>2</sub>O<sub>3</sub>).

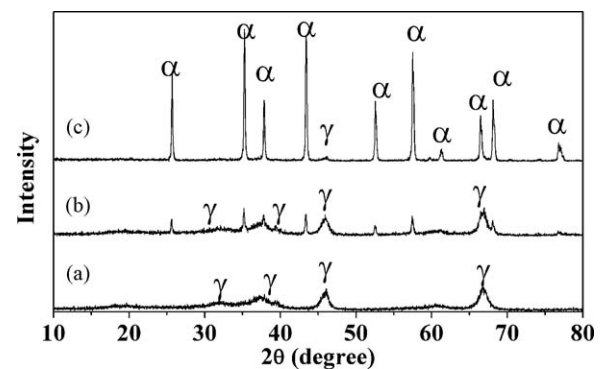


Fig. 3. XRD patterns for sample 0T4K calcined at various temperatures (a) 800 °C, (b) 900 °C and (C) 1000 °C ( $\alpha$ , $\alpha$ -Al<sub>2</sub>O<sub>3</sub>,  $\theta$ , $\theta$ -Al<sub>2</sub>O<sub>3</sub>,  $\gamma$ , $\gamma$ -Al<sub>2</sub>O<sub>3</sub>).

diffusion. For boehmite co-doped with 1 mol% Ti<sup>4+</sup> and 5 mol% Fe<sup>3+</sup> (sample 1T), the phase transformation temperature further decreased to 1030 °C (Fig. 1(d)). This agrees with literature [17] that Ti<sup>4+</sup> entered Al<sub>2</sub>O<sub>3</sub> substitutionally, which resulting in the increase in V<sub>Al</sub><sup>'''</sup> concentration, thereby promoting  $\gamma \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> phase transformation. The broad exothermic peak observed at 700–900 °C can be ascribed to  $\gamma \rightarrow \delta \rightarrow \theta$ -Al<sub>2</sub>O<sub>3</sub> phase transformation, which can be confirmed by XRD results shown in Fig. 2. For sample 1T added with K<sub>2</sub>SO<sub>4</sub>, 1T4K, the endothermic peak occurring at about 598 °C is associated with the transformation from the

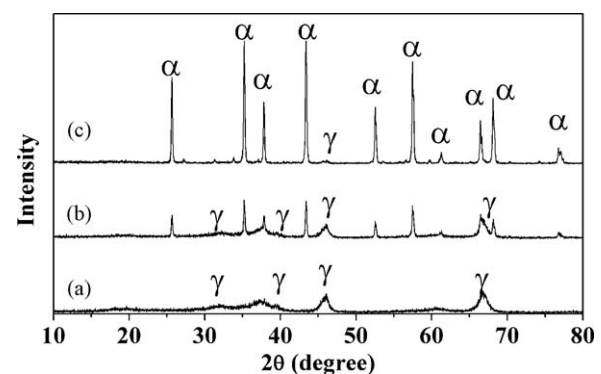


Fig. 4. XRD patterns for sample 1T4K calcined at various temperatures (a) 800 °C, (b) 900 °C and (C) 1000 °C ( $\alpha$ , $\alpha$ -Al<sub>2</sub>O<sub>3</sub>,  $\theta$ , $\theta$ -Al<sub>2</sub>O<sub>3</sub>,  $\gamma$ , $\gamma$ -Al<sub>2</sub>O<sub>3</sub>).

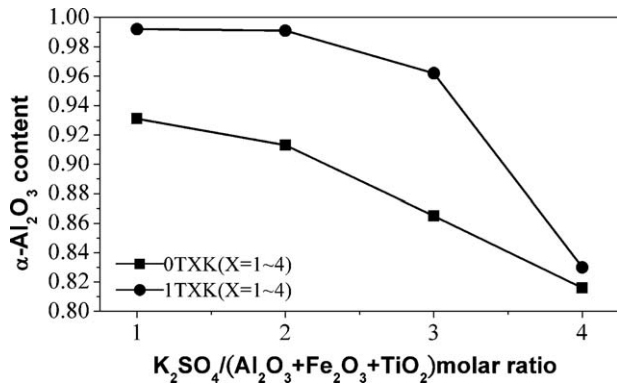


Fig. 5. Effect of different added molar ratio of potassium sulfate on  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> formation.

orthorhombic (low temperature form) to the hexagonal phase (high temperature form) of K<sub>2</sub>SO<sub>4</sub>, the endothermic peak at 1067 °C is due to the melting of K<sub>2</sub>SO<sub>4</sub>, and no other exothermic peak originated from Al<sub>2</sub>O<sub>3</sub> phase transformation was observed (Fig. 1(a)). Figs. 3 and 4 show the XRD patterns

for samples 0T4K and 1T4K calcined at various temperatures. Comparison of the XRD patterns for the samples with and without K<sub>2</sub>SO<sub>4</sub> addition (Figs. 2–4), shows that K<sub>2</sub>SO<sub>4</sub> addition changed Al<sub>2</sub>O<sub>3</sub> phase transformation from  $\gamma \rightarrow \delta \rightarrow \theta \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub> to  $\gamma \rightarrow \alpha$ -Al<sub>2</sub>O<sub>3</sub>, avoiding the transition via  $\theta$ -Al<sub>2</sub>O<sub>3</sub>.

### 3.2. Effects of addition of K<sub>2</sub>SO<sub>4</sub> on the formation and anisotropy of $\alpha$ -Al<sub>2</sub>O<sub>3</sub>

Fig. 5 shows the effect of different added molar ratio of potassium sulfate on  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> formation. The results indicate that the amount of  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> formation decreased gradually with increasing K<sub>2</sub>SO<sub>4</sub> addition of. It was found [18]  $\theta$ - to  $\alpha$ -phase transformation of Al<sub>2</sub>O<sub>3</sub> to occur when  $\theta$ -Al<sub>2</sub>O<sub>3</sub> crystallite exceeds a critical size  $d_c$ ,  $\theta = 20$ –25 nm upon heating to a temperature above 1000–1150 °C. Recently, many researches have added a salt as a diluent to the starting materials and then calcined the mixture at temperatures below the salt melting temperature [19–20]. It was found that salt can separate the nano-particles and prevent crystallite growth and agglomera-

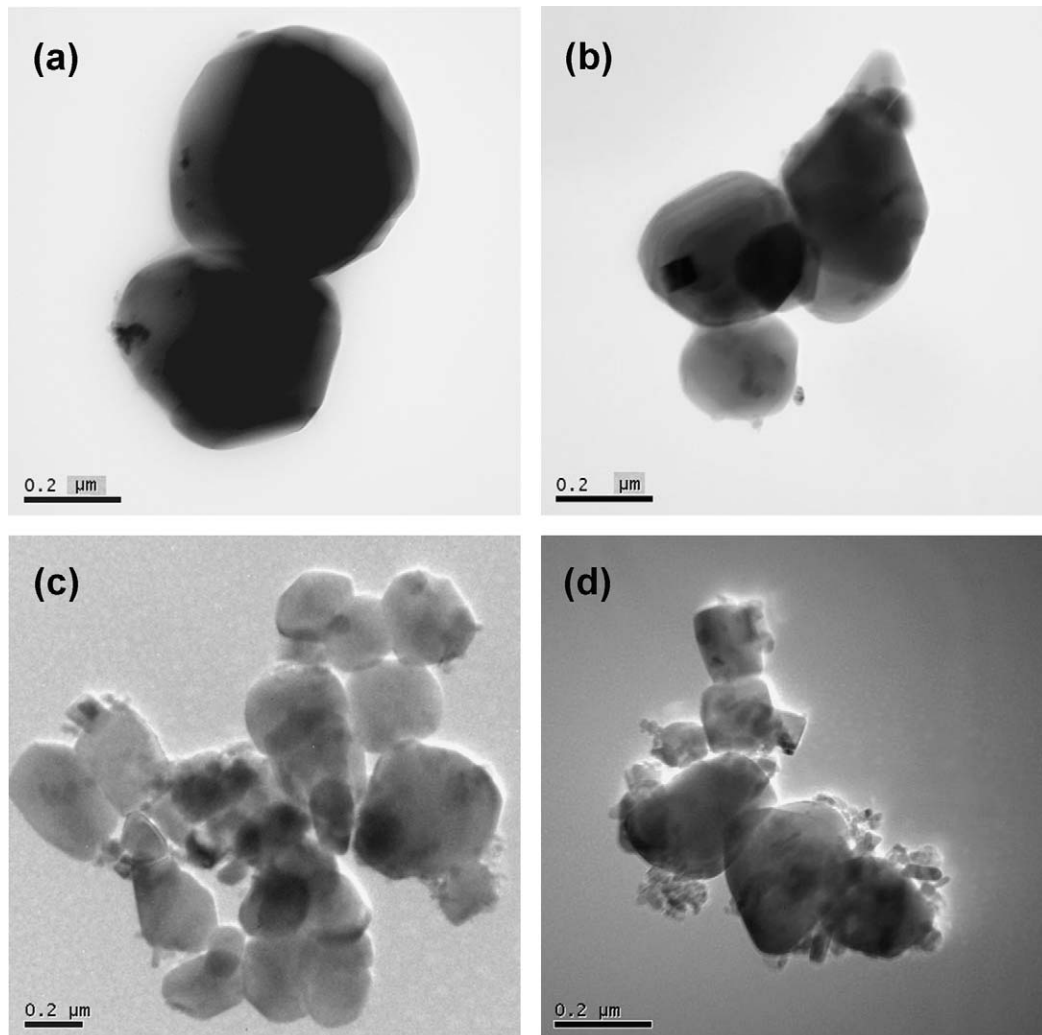


Fig. 6. TEM micrographs of sample 1T added with various K<sub>2</sub>SO<sub>4</sub> molar ratios and calcined at 1000 °C for 2 h (a) 1T1K, (b) 1T2K, (c) 1T3K and (d) 1T4K.

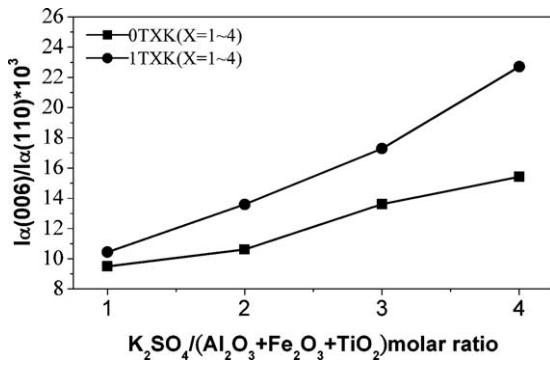


Fig. 7. Variation of  $I_{(0\ 0\ 6)}/I_{(1\ 1\ 0)}$  for the samples with various amounts of  $K_2SO_4$ .

tion. The effect of monovalent cation additives on  $\gamma \rightarrow \alpha$ - $Al_2O_3$  was found to form a surface amorphous phase formed by the addition of  $K^+$  cations which suppresses the growth of  $\gamma$ - $Al_2O_3$  grains and retards  $\alpha$ - $Al_2O_3$  formation [21]. Because the calcination temperature ( $1000\ ^\circ C$ ) was below the  $K_2SO_4$  melting temperature ( $1067\ ^\circ C$ ) in this study,  $K_2SO_4$  may act

as a solid barrier to separate  $\gamma$ - $Al_2O_3$  and to prevent crystallite growth, resulting in some  $\gamma$ - $Al_2O_3$  crystallites not reaching the critical phase transformation size, thereby surviving after calcination. Fig. 6 shows TEM micrographs of sample 1T added with various  $K_2SO_4$  molar ratios and calcined at  $1000\ ^\circ C$  for 2 h. For sample 1T1K, the powders consist of crystallites  $0.4$ – $0.5\ \mu m$  in size, which are opaque to electrons. With increasing potassium sulfate addition, the electron transparency of the crystallites increased, indicating the crystallite shape to gradually change from granular to flaky. In addition, for sample 1T4K, the proportion of the  $\gamma$ - $Al_2O_3$  crystallites with size less than  $20\ nm$  is higher than for the other samples, which is consistent with the XRD result (Fig. 4). The  $\alpha$ - $Al_2O_3$  shape anisotropy can be semi-quantitatively determined by calculating  $I_{(0\ 0\ 6)}/I_{(1\ 1\ 0)}$ , where  $I_{(0\ 0\ 6)}$  and  $I_{(1\ 1\ 0)}$  are the integrated XRD intensities of the  $(0\ 0\ 6)$  peak and  $(1\ 1\ 0)$  peak of  $\alpha$ - $Al_2O_3$ , respectively. Fig. 7 shows the variation of  $I_{(0\ 0\ 6)}/I_{(1\ 1\ 0)}$  for samples with various amounts of  $K_2SO_4$ , showing that the  $\alpha$ - $Al_2O_3$  shape anisotropy increased with increasing  $K_2SO_4$  addition. From the above results, it can be concluded that  $K_2SO_4$  addition acts as a diluent to separate the nanoparticles

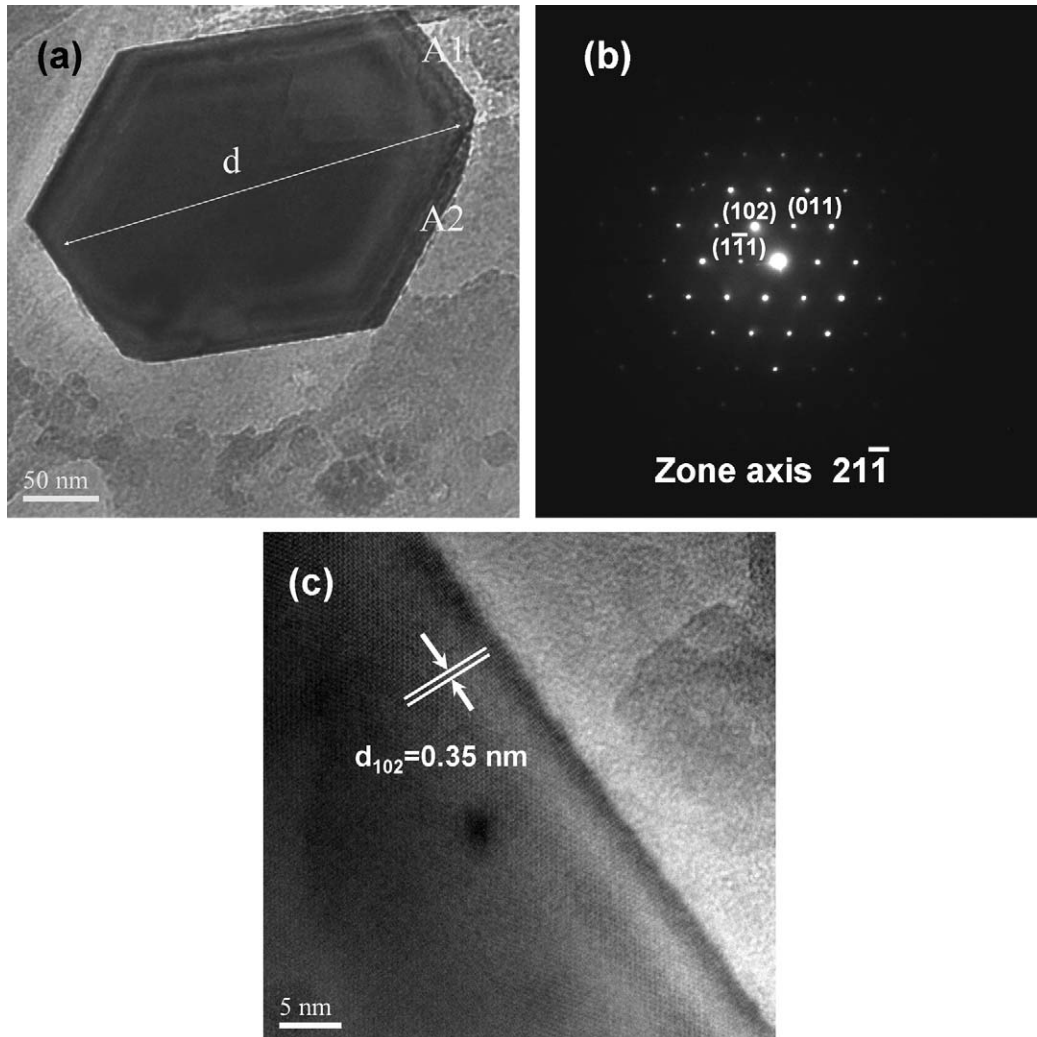


Fig. 8. (a) TEM bright field image, (b) corresponding to selected area of the electron diffraction pattern and (c) high resolution lattice image at A1 for sample 0T4K.

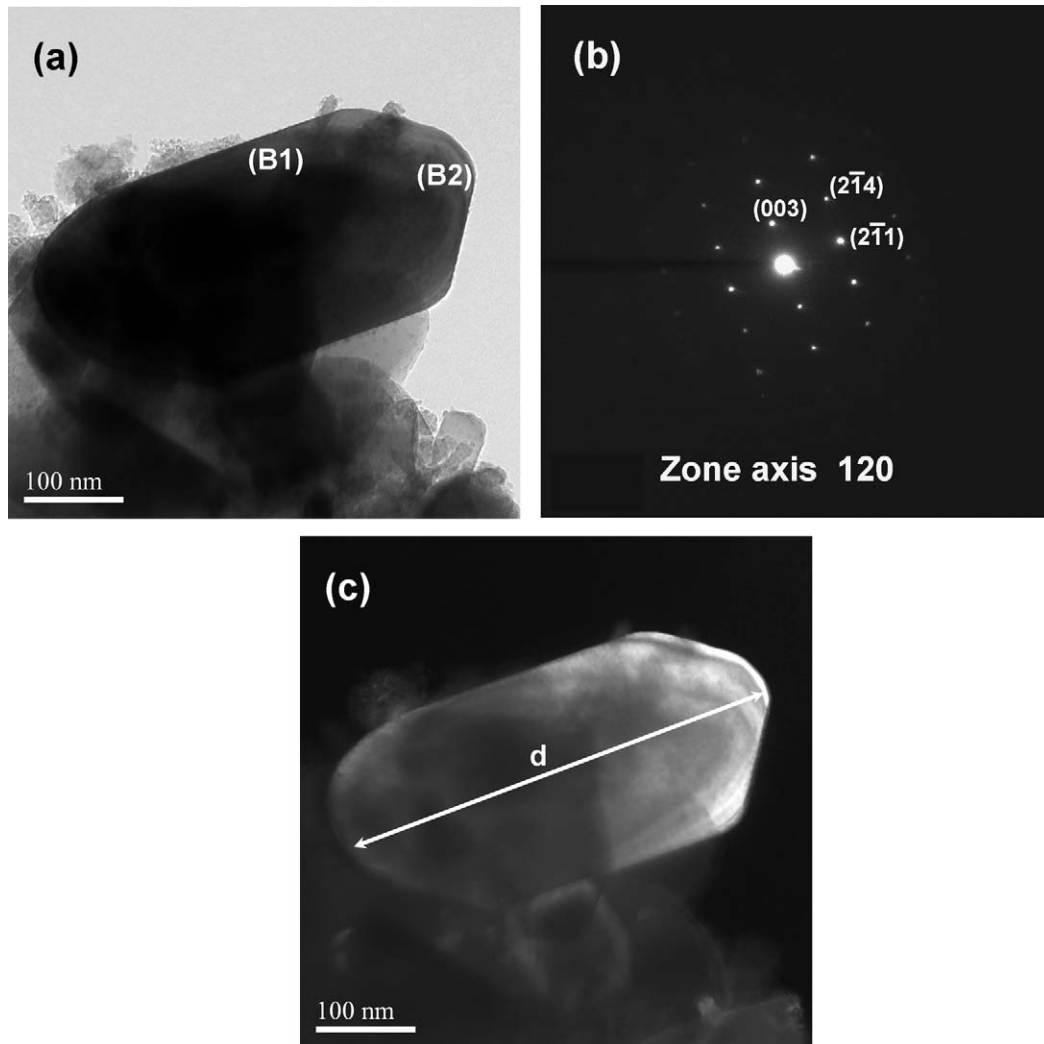


Fig. 9. (a) a TEM bright field image, (b) corresponding to selected area of the electron diffraction pattern (SAEDP) and (c) dark field image for sample 1T4K calcined at 1000 °C for 2 h.

and prevent crystallite growth and also promotes the anisotropic crystallite growth, thereby enhancing flaky  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> crystallite formation.

### 3.3. Effect of Ti<sup>4+</sup> addition on the anisotropic crystallite growth

Fig. 8(a and b) shows a TEM bright field image and corresponding selected area electron diffraction pattern (SAEDP) for sample 0T4K, respectively. The regular hexagonal pattern and strong diffraction spots indicate an excellent single crystal structure in the platelet, which could be indexed as  $\alpha$ -Al<sub>2</sub>O<sub>3</sub>. Fig. 8(c) shows the high-resolution lattice image at A1 (in Fig. 8(a)) with a clearly resolved lattice fringe of the (1 0 2) planes ( $d = 0.348$  nm), further confirming the single crystalline nature of each flaky crystallite. Moreover, the chemical composition of this region, as confirmed by EDS is shown in Table 2, which is close to the nominal composition. Fig. 9(a–c) shows a TEM bright field image, corresponding selected area electron diffraction pattern (SAEDP), and dark

field image for sample 1T4K calcined at 1000 °C for 2 h, respectively, indicating the hexagonal flaky crystallite to be a single  $\alpha$ -Al<sub>2</sub>O<sub>3</sub> crystal. Comparison of Figs. 8 and 9 indicate that Ti<sup>4+</sup> addition can promote the anisotropic crystallite growth of flaky  $\alpha$ -Al<sub>2</sub>O<sub>3</sub>. Fig. 10 shows the high-resolution lattice image at B1 and B2 (in Fig. 9(a)) with a lattice fringe of the (0 0 3) planes ( $d = 0.43$  nm) and (2–11) planes ( $d = 0.234$  nm). In addition, the chemical composition of this region was confirmed by EDS and shown in Table 2. These results indicate that Ti<sup>4+</sup> ions tend to segregate onto the surface of (0 0 3) basal planes, which promotes the anisotropic crystallite growth. This

Table 2  
Chemical compositions of the different regions detected by EDS.

Area	Element (atom%)		
	Al K	Ti K	Fe K
Al	93.86	–	6.14
B1	88.33	5.00	6.67
B2	91.65	1.31	7.04

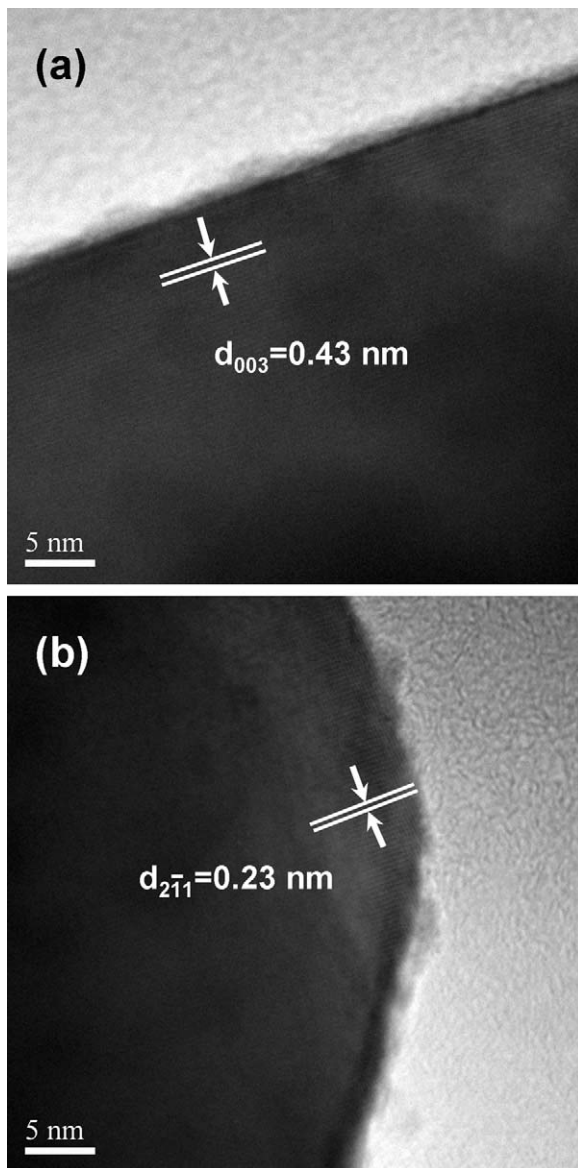


Fig. 10. High-resolution lattice image at (a) B1 and (b) B2 (in Fig. 9(a)) with a lattice fringe of the (0 0 3) planes ( $d = 0.43$  nm) and ( $2 \bar{1} 1$ ) planes ( $d = 0.234$  nm).

is supported by previous findings [22] indicating the tendency of  $\text{TiO}_2$  to segregate at the grain boundary where it may hinder the growth of specific surfaces, thereby enhancing the development of platelet-shaped alumina grains.

#### 4. Conclusions

- i. Flaky single-crystal  $\alpha\text{-Al}_2\text{O}_3$  can be obtained by heating a mixture of  $\text{Fe}^{3+}$ -doped boehmite and potassium sulfate at  $1000^\circ\text{C}$ .
- ii.  $\text{K}_2\text{SO}_4$  addition acts as a diluent to separate the nanoparticles and prevent crystallite growth, and also promotes the anisotropic crystallite growth.
- iii.  $\text{Ti}^{4+}$  ions tend to segregate onto the surface of (0 0 3) basal planes, which promotes anisotropic crystallite growth, thereby enhancing flaky  $\alpha\text{-Al}_2\text{O}_3$  crystallite formation.

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